# CHANCE News 13.05 June 8, 2004 to November 1,2004

Prepared by J. Laurie Snell, Bill Peterson, Jeanne Albert, and Charles Grinstead with help from Fuxing Hou and Joan Snell. We are now using a listserv to send out notices that a new Chance News has been posted on the Chance Website. You can sign on or off or change your address at <u>here.</u> This listserv is used only for this posting and not for comments on Chance News. We do appreciate comments and suggestions for new articles. Please send these to jlsnell@dartmouth.edu.

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I returned, and saw under the sun, that the race [is] not to the swift, nor the battle to the strong, neither yet bread to the wise, nor yet riches to men of understanding, nor yet favour to men of skill; but time and chance happeneth to them all.

Ecclesiastes 9.11

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In his <u>article</u> Paulos pointed out that, when we transform these into probabilities they have a sum of 1.68. Dan Seligman made a similar observation in his article <u>Why Journalists Can't Add</u> in *Forbes Magazine*. But Granberg reminds us that when bookies make odds it is standard practice to have the corresponding probabilities add to more than one. Indeed, that is how the bookies make their money. And when presenting these odds, Safire writes: "Here is the early-morning line handicapped by one right-wing tout." So Safire is referring to gambling odds. Admittedly a probability of 1.68 would be a pretty greedy bookie but since Safire is probably the bookie that's his privilege. Granberg checked a number of gambling odds and found, for example, that the odds for the 32 NFL football teams winning the 2005 Superbowl added up to 1.31 which he thought was a bit excessive.

#### Bush? Kerry? Why pollsters cannot agree. *The New York Times*, October 19, 2004, Page 1 Jim Rutenberg

While the headline of this article suggests that recent presidential polls have produced significantly different results, by the fourth paragraph the author admits that "the actual findings of these polls may not be so different." To help explain these apparent differences, several potential factors are mentioned, including political motives by pollsters, survey methodology, caller ID systems that can easily screen incoming calls, and increasing cell phone use (cell phones are not included in random phone samples). The main focus of the article, however, is the different ways that pollsters attempt to determine if a person will actually vote.

Most political polls report the responses of either registered voters or "likely" voters. A <u>chart</u> that accompanies the article first displays, for five recent polls, the percentages of registered voters that favor Kerry and that favor Bush. The results range from equal percentages for each candidate to a 3% lead for Bush. As noted in the article, in each case the gap between the percentages for each Candidate are within the margin of error (3 or 4%) of the given poll.

Next, the chart displays the results for "likely" voters, which show greater gaps between the percentages favoring each candidate. Although for three polls the gaps are still within the margin of error, the remaining two report more dramatic differences: an eight-point lead for Bush in the CNN/*USA Today*/Gallup poll (up from a three-point lead among registered voters), and a six-point lead for Bush in the *Newsweek* poll (up from a two-point lead.) All the polls were conducted over two to four days during the period October 14 to October 17.

How do the different polling organization determine who is a "likely" voter? And how might different methods produce such apparently different results? While the exact procedures are not described, the article does indicate some differences between the methods used by Gallup and by the *New York Times*/CBS poll. (The former poll reports 49% for Bush and 46% for Kerry among registered voters; for "likely" voters the figures are 52% Bush, 44% Kerry. The latter poll has Bush and Kerry tied at 45% among registered voters; among "likely" voters it's Bush 47%, Kerry 45%. (These figures have undoubtedly changed by the time you are reading this.) Both organizations use responses to questions about, for example, voting history and relative interest in the election, as indicators of voting likelihood. Gallup uses these responses to gauge voter turnout, and "after estimating what the actual turnout will be," the article states, "Gallup includes the preferences of just that fraction of their respondents. The New York Times and CBS, on the other hand, include responses from all those determined to be likely voters, but gives some of their votes more weight than others," depending on the level of likelihood indicated. Unfortunately, without further information, it is difficult to gauge the potential impacts of the two methods.

The pollster John Zogby has recently raised two issues not discussed in this article: the effect of differing distributions of Republicans, Democrats, and Independents across different polls, and response rates.

Polls from early September by both *Time* and *Newsweek* showed 11% leads for Bush, while Zogby's poll had Bush ahead by 2%. (See "2004: It is not an 11 point race".) Zogby concludes that this difference derives from the distribution of party affiliation in the samples. According to Zogby, the *Newsweek* poll of registered voters consisted of 38% Republicans, 31% Democrats, and 31% Independents. On the other hand, Zogby's organization weights each party to reflect the party distribution in recent presidential elections: 35% Republicans, 39% Democrats, and 26% Independents. (This is the same as the distribution that Zogby gives for 2000; for 1996 he has 34% Rep., 39% Dem., 27% Ind.) While Zogby is clearly not a disinterested party, his point is worth exploring and it is surprising (or is it?) that the *Times* article missed it.

Except for comments regarding the prevalence of caller ID systems and cell phone use, the *Times* article does not discuss response rates. In a recent lecture given at SUNY Potsdam, Zogby remarked that when he started his polling career, response rates were around 60%. Today, he said, they are under 30%, and only 8-10% in metropolitan areas. (Audio of the lecture is available <u>here</u>. Response rates were discussed during the Q&A, which is in a separate audio file on the same site). He also noted that his organization has been developing "interactive", or internet polling methods, and that he expects polling to move in this direction.

One such national poll is already up and running: the <u>YouGov poll</u>, commissioned by the *Economist* magazine, which uses a panel of 10,000 e-mail addresses from which it selects its samples. (More information about their methods and results, including an overview of current problems with phone surveys, is available at the <u>Economist</u> website.)

## **<u>Puzzler: One seat left. Is it yours</u>?** Car Talk, 4 October 2004

This week's Car Talk puzzle asked:

One hundred people line up to board an airplane, but the first has lost his boarding pass and takes a random seat instead. Each subsequent passenger takes his or her assigned seat if available, otherwise a random unoccupied seat. You are the last passenger. What is the probability that you get your own seat?

You and your students would enjoy this puzzle if you have not seen it before. It has not made Marilyn's column yet but it is in Peter Winkler's very nice new book: <u>Mathematical Puzzles: A Connoisseur's Collection</u> where it is called "The lost boarding pass puzzle." You can find the <u>solution</u> to this puzzle at the end of this Chance News.

This puzzle also appeared in the <u>March/April 2003</u> issue of the Journal *Contingencies*. This journal is published quarterly by the <u>American Academy of Actuaries</u> and includes a puzzle column edited by Noam Segal. Not surprisingly, these puzzles often involve probability or statistical concepts.You can see the current puzzle and the answer to the previous puzzle at the <u>Contingencies website</u>. Earlier puzzles are archived at the <u>Nebraska Actuaries</u> <u>Club website</u>. You will find other questions relating to the lost boarding pass puzzle in the <u>May/June 2003</u> issue and the solutions to these and the original puzzle in the <u>July/August</u>, 2003 issue. We include two of these in our discussion questions.

## **DISCUSSION QUESTIONS:**

(1) What is the expected number of people who get their own seats?

(2) Under the same conditions as the original problem what is the probability the last person gets his/her own seat if the first two people lose their boarding passes?

## The impact of No Child Left Behind (graphic). *New York Times*, 17 August, 2004

This <u>data graphic</u> appeared in the *Times*. It is intended to compare two variables at the state level: percentage of schools facing penalties under the No Child Left Behind Act, and percentage with fourth graders not meeting the basic reading standard.

DISCUSSION QUESTIONS:

1. Do you understand think the graphic makes the intended comparison clear? Can you suggest another way to present the data?

2. What consequences might there be in aggregating the data in this way?

#### The politics of terrorist warnings (Or, who's afraid of orange alerts?). *Washington Post*, 5 September 2004, B05 Richard Morin

In this election year, the threat of terrorism has been widely viewed as a plus for the Bush campaign. Darren Davis and Brian Silver, two political scientists from the University of Michigan researchers, have questioned this view in a paper entitled <u>The Threat of Terrorism</u>, <u>Presidential Approval</u>, and the 2004 Election.

Their study examines the relationship between President Bush's approval rating and public fears of terrorism. It draws on two national surveys and a series of surveys done in Michigan between 2001 and 2004. In 2001, after the 9/11 attacks, people who expressed higher levels of concern about terrorism were more likely to approve of the President. In 2004, however, there is evidence that the association may have reversed direction. The *Post* article reports that:

In the latest Michigan statewide survey, completed in June, 64 percent of those who were "not at all concerned" about terrorism approved of the job Bush was doing as president. But among those who were "very concerned" about the possibility of another terrorist attack, only 26 percent thought the president was doing a good job....

The researchers also report that while the government's system of color-coded terror warning does affect people's perception of the threat level, the posting of new warnings does not appear to affect the President's approval rating.

**Economists venture Olympic predictions.** NPR, Morning Edition, 9 Aug. 2004.

<u>Predicting countries' medal counts at the olympics.</u> Morning Edition, 1 Sept. 2004 John Vdstie

**Medal Miscount** Slate Magazine, August 30, 2004

Greece	16	27	13	11	3
South Korea	30	27	28	3	2
Cuba	27	25	29	2	2
Romania	19	23	26	4	7
Netherlands	22	21	25	1	3
Ukraine	23	20	23	3	0
Japan	37	19	18	18	19
Hungary	17	14	17	3	0
Belarus	15	13	17	2	2
Canada	12	13	14	1	2
Poland	10	12	14	2	4
Brazil	10	12	12	2	2
Spain	19	11	11	8	8
Sweden	7	11	12	4	5
Bulgaria	12	10	13	2	1
Norway	6	8	10	2	4
Switzerland	5	8	9	3	4
Czech Republic	8	6	8	2	0
Mexico	4	6	6	2	2
Indonesia	4	6	6	2	2
Ethiopia	7	5	8	2	1
Kazakhstan	8	5	7	3	1
Denmark	8	5	6	3	2
Kenya	7	4	7	3	0
Jamaica	5	3	7	2	2
Georgia	4	3	6	1	2
Average				4	3.56

We see the Chance class method did slightly better on the average absolute error. Another measure of success suggested by Barnard and Russe is the correlation between the number of medals predicted and the number won. Using the above data we obtain a correlation of .976 for Barnard-Busse and .977 for the Chance class. Thus, by these two measures, the two methods of predictions appear to be equally effective in predicting the number of medals won.

Similar predictions for the 2000 and 2004 summer olympics were made by Dan Johnson and Ayfer Ali[4]. Johnson and Ali use economic and political variables similar to those used by Bernard and Busse except for the important difference that they did not use outcome of the previous olympics as a variable. They wanted to concentrate on the ability to predict the outcomes from political and economic variables.

Still a third study was referred to in the Slate article. It was carried out by John Hawksworth, Jon Bunn, and Kate

Alexander of PricewaterhouseCoopers in the UK. These authors used political and economic variables similar to the other studies and also included previous olympic performance. Unfortunately, they do not provide the details of their regression.

Each study had its own way to determine which countries to use to test their predictions. The Barnard-Russe study chose all those countries who won at least 6 medals in the previous summer olympics which gave them 34 countries. The PwC study chose the top 30 countries according to it's own predictions. The Johnson-Ali study had predictions only for countries for which they were able to get the economic and political data needed for their regression. In comparing the Chance class predictions with those of this study, we compared predictions for countries for which Johnson-Ali study the required data and that won at least 4 medals in the previous summer olympics. This gave us 30 countries for this comparison. We used the correlation R and the mean absolute error to compare each studies' predictions with the Chance class predictions for the same group of countries. Since the studies do not use the same countries for their predictions, the Chance class had different results for each of the three studies. Here are the results:

	Bernard Busse	Chance class	PwC	Chance Class	Johnson Ali	Chance class
Correlation R	.976	.977	.970	.971	.913	.977
Mean absolute error	4	3.56	6.9	3.8	7.97	3.87

We see that the Chance class always does slightly better on the correlation and perhaps significantly better on the mean absolute error. Note that the Johnson Ali predictions have an impressive correlation even without using previous performance. Unlike the others Johnson and Ali also look at the winter olympics and make comparisons with the summer olympic. They are also are the only ones who explained their methodology in a way that we could understand.

## **References.**

(1) Going for the gold: Who will win the 2004 Olympic games in Athens? Andrew B. Bernard, Meghan R. Busse, July, 2004

(2) Who wins the olympic games: Economic resources and medal totals. The Review of Economics and Statistics, February 2004, 86(1):413-417

(4)A Tale of Two Seasons: Participation and Medal Counts at the Summer and Winter Olympic Games To appear December 2004 in Social Science Quarterly. Daniel K.N. Johnson and Ayfer Ali January 2002

<u>The Chance Manifesto.</u> Draft Version .3, 2 June 2004 Peter Doyle

<u>Clinical trial registration</u>: A statement from the International Committee of Medical Journal Editors.

## New England Journal of Medicine, 351;12, 16 September 2004

## Medical journals want more transparent research data.

NPR: Talk of the Nation, 10 September, 2001 Ira Flatow with Guest Dr. Catherine DeAngelis, editor-in-chief JAMA

#### <u>Legislators propose a registry to track clinical trials from start to finish.</u> *Science*, Vol 305, Issue 5691,1695, 17 September 2004 Jennifer Couzin

In his Chance Manifesto, Peter gives an example to show the difficulty in assessing the value of a statistical experiment without knowing what the experimenter planned to do before the experiment was conducted. Peter proposes that this information should be made publicly available. He writes

Now the interesting thing is that there is already a mechanism in place for registering in advance of a study what data is to be collected and how the data is to be analyzed. This mechanism is mandated by the federal government for any studies involving human subjects funded by the US Department of Health and Human Services, and separately, for studies of any drugs, medical devices, etc. regulated by the Food and Drug Administration. This means that investigators are already being forced to commit themselves in advance to how they are going to run their experiments

Peter then discusses why a researcher might want this information to be made publicly available. He writes

If I were a funding agency, or a reviewer for a funding agency, I would look kindly on investigators who have an established policy of archiving the plans of their investigations in advance. Such a policy would impress me as a sign of honorable intent, and just as important, it would give me a way to check over their track record. Turning from the investigator to the particular investigation, I would look kindly on proposals whose study plans were either already archived, or (more likely) where there was a commitment to archive the plans before the start of the study. In fact, if I were in a position to do so, I would make funding contingent on pre-archiving any study paid for in whole or in part with the funds being allocated.

Other parties who could benefit from a pre-archiving scheme would be the journals where results of studies are published. If I were a medical journal editor, I would look kindly on studies that were archived in advance. In fact, if I were an editor, I would consider for publication only studies archived in advance, and if I were a reviewer, I would consent to review only studies that had been archived in advance.

As if they had been listening to Peter, the *International Committee of Medical Journal Editors* (ICMJE) representing eleven prestigious Medical Journals including the *New England Journal of Medicine, Journal of the American Medical Association*, and *Lancet*, announced that member journals of the ICMUE will, as a condition of consideration for publication, require registration in a public trials registry at or before the onset of patient enrollment. You can find their statement <u>here</u>. In describing the requirements for the registry we read:

The ICMJE does not advocate one particular registry, but its member journals will require authors to register their trial in a registry that meets several criteria. The registry must be accessible to the public at no charge. It must be open to all prospective registrants and managed by a not-for-profit organization. There must be a mechanism to ensure the validity of the registration data, and the registry should be electronically searchable.

An acceptable registry must include at minimum the following information: a unique identifying number, a statement of the intervention (or interventions) and comparison (or

comparisons) studied, a statement of the study hypothesis, definitions of the primary and secondary outcome measures, eligibility criteria, key trial dates (registration date, anticipated or actual start date, anticipated or actual date of last follow-up, planned or actual date of closure to data entry, and date trial data considered complete), target number of subjects, funding source, and contact information for the principal investigator.

To our knowledge, at present, only www.clinicaltrials.gov, sponsored by the United States National Library of Medicine, meets these requirements; there may be other registries, now or in the future, that meet all these requirements.

<u>ClinicalTrials.gov</u>, founded by the NIH with the FDA, was a result of the <u>1997 FDA Modernization Act</u> (FDAMA). This act required that clinical trials related to life threatening illnesses be registered and be available to the general public so that people with these illnesses could find out how to enroll in a related clinical trial. The Act defined a clinical trial as "a research study in human volunteers to answer specific health questions" and so includes observational studies, trials with or without control groups etc. Also it has been expanded and is not limited to trials relating to life threatening-illnesses. It is a very well-run register and currently has listed about 11,000 studies.

However the FDA Modernization Act did provide an enforcement mechanism so it does not include all the trials that the law requires. A review by FDA staff showed that between January and September 2002, 91% of government-sponsored cancer studies that fall under the Act had been registered, as compared with 49 percent of industry-sponsored trials.

In the <u>NPR Talk of the Nation program</u> Catherine DeAngelis, editor-and-chief of JAMA explains why the Journals were led to their new policy and the information they will require in the registration. She was asked by Ira and by listeners if they are also requiring that the results of the study be made available. DeAngelis said no that that they did not feel that they could require this. She said that they do not expect the public to use this registration but it will permit the editors, when they receive a paper, to see what other studies have been started and they will then be able to find out from the principle investigator the results of these studies. This will help them decide if a paper should be accepted, and if accepted, it will help the editors provide, in an editorial, the significance of the study in the context of the results of other related studies. This did not satisfy one of the listeners.

The issue of the public's right to know the outcomes of studies was also in the news because of the controversy over the question of the use of antidepressant drugs in the treatment of children.

The New York State attorney, Eliot Spitzer, sued the British drug company GlaxoSmithKline charging that the company had not disclosed the results of clinical trials of their antidepressant drug Paxil that failed to show the drug was effective in treating children and adolescents and that suggested a possible increase of risk of suicide. The suit was based on the results of three studies paid for by GSK to see the effect of Paxil on treating major depression in children and adolescents.

GSK study	Final report	Suicidal ideation <sup>*</sup> on Paxil	Suicidal ideation <sup>*</sup> on placebo
329, M. Keller <i>et al</i>	. 2001	5.8%	1.8%
377	1998–99	4.8%	10.6%
701	2000	18.8%	16.0%

# **GSK's Reanalysis of Risks**

<sup>\*</sup> Emergent suicidal ideation includes self-injurious remarks or behaviors related to suicidal ideation, suicide attempts, self-inflicted harm, or overdoses.

Only study 329 was published. The suit claimed that none of the results were significant and charges GSK with publicizing the apparent favorable study 377 and suppressing information about the other two studies that suggested that the drug had no effect on behavior related to suicides. Spitzer provided internal memos and letters to Doctors to support this claim. You can find their lawsuit <u>here</u>. The suit was settled in September with the company paying 2.5 million dollars and agreeing to post online both negative and positive results from its clinical drug trials.

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These developments led Representatives Edward Markey and Henry in the House and Senators Chris Dodd and Edward Kennedy in the Senate to plan to introduce legislation that would require pharmaceutical companies to post clinical trial information publicly. They are proposing requiring the posting of information similar to that required by the Medical Journals but also requiring that the results be promptly reported. The legislation proposed by Markey and Henry is available here.

## **DISCUSSION QUESTIONS:**

(1) An article available <u>here</u> discusses first amendment issues related to requiring companies to post results of their studies. The article concludes with the remark:

Compulsory disclosure of all clinical trial results poses a real danger that pharmaceutical companies will simply cut short those tests that might be headed toward negative or inconclusive results, to the detriment of medical science in the short term and in the long run to the public health in general. The Spitzer Complaint and any others to follow are simply ill-conceived.

Do you think this is a concern?

Paul Meagher provided the next article. Paul has an interesting web site <u>phpmath</u>. Since PHP has not yet become a household word we asked Paul to write a one sentence description of PHP and his site. He wrote:

PHP is a popular opensource programming language that is particularly suited for serverside Web application programming. The goal of the opensource site www.phpmath.com is offer a library of high-quality PHP source code for mathematical programmers often with a view towards use in Web applications.

A good example of how PHP is used to solve a statistical problem related to the web can be found at <u>Conduct Web</u> experiments using PHP, Part 1.

But on to Paul's contribution. Paul reviews the following book:

#### The Smoking Puzzle: Information, Risk Perception and Choice. Harvard University Press, May 2003, 288 pages, \$55 Frank A. Sloan, V. Kerry Smith, Donald H. Taylor, Jr.

Why do people persist in a self-destructive behavior such as smoking?

Depending on your background, you will regard the possible answers (e.g., addiction, genetic predisposition, peer pressure, stress relief, weight control, utility maximization, etc...) as more or less self-evident. If you are an


http://home.uchicago.edu/~gbecker/

#### hrsonline.isr.umich.edu/

#### <u> The Wisdom of Crowds</u>

here

review

<u>http://</u>

#### One vote, one value

A certain class of problems do not as yet appear to be solved according to scientific rules, though they are of much importance and of frequent recurrence. Two examples will suffice. (1) A jury has to assess damages. (2) The council of a society has to fix on a sum of money, suitable for some particular purpose. Each voter, whether of the jury or of the council, has equal authority with each of his colleagues. How can the right conclusion be reached, considering that there may be as many different estimates as there are members? That conclusion is clearly not the average of all the estimates, which would give a voting power to "cranks" in proportion to their crankiness. One absurdly large or small estimate would leave a greater impress on the result than one of reasonable amount, and the more an estimate diverges from the bulk of the rest, the more influence would it exert. I wish to point out that the estimate to which least objection can be raised is the *middlemost* estimate, the number of votes that it is too high being exactly balanced by the number of votes that it is too low. Every other estimate is condemned by a majority of voters as being either too high or too low, the middlemost alone escaping this condemnation. The number of voters may be odd or even. If odd, there is one middlemost value: thus in 11 votes the middlemost is the 6th; in 99 votes the middlemost is the 50th. If the number of voters be even, there are two middlemost values, the mean of which must be taken; thus in 12 votes the middlemost lies between the 6th and the 7th; in 100 votes between the 50th and the 51st. Generally, in 2n-1 votes the middlemost is the *n*th; in 2n votes it lies between the *n*th and the (n+1)th.

I suggest that the process for a jury on their retirement should be (1) to discuss and interchange views; (2) for each juryman to write his own independent estimate on a separate slip of paper; (3) for the foreman to arrange the slips in the order of the values written on them; (4) to take the average of the 6th and 7th as the verdict, which might be finally approved as a substantive proposition. Similarly as regards the resolutions of councils, having regard to the above (2n-1) and 2n remarks.

Francis Galton

#### Vox populi

In these democratic days, any investigation into the trustworthiness and peculiarities of popular judgments is of interest. The material about to be discussed refers to a small matter, but is much to the point.

A weight-judging competition was carried on at the annual show of the West of England Fat Stock and Poultry Exhibition recently held at Plymouth. A fat ox having been selected, competitors bought stamped and numbered cards, for 6*d*, each, on which to inscribe their respective names, addresses, and estimates of what the ox would weigh after it had been slaughtered and "dressed" Those who guessed most successfully received prizes. About 800

tickets were issued, which were kindly lent me for examination after they had fulfilled their immediate purpose. These afforded excellent material. The judgments were unbiassed by passion and uninfluenced by oratory and the like. The sixpenny fee deterred practical joking, and the hope of a prize and the joy of competition promoted each competitor to do his best. The competitors included butchers and farmers, some of whom were highly expert in judging the weight of cattle; others were probably guided by such information as they might pick up, and by their own fancies. The average competitor was probably as well fitted for making a just estimate of the dressed weight of the ox, as an average voter is of judging the merits of most political issues on which he votes, and the variety among the voters to judge justly was probably much the same in either case.

After weeding thirteen cards out of the collection, as being defective or illegible, there remained 787 for discussion. I arrayed [see Table 1] them in order of the magnitudes of the estimates, and converted the *cwt.*, *quartors*, and *lbs.* in which they were made, into lbs., under which form they will be treated.

According to the democratic principle of "one vote one value," the middlemost estimate expresses the *vox populi*, every other estimate being condemned as too low or too high by a majority of the voters (for fuller explanation see "One vote, one value," *Nature*, February 28, p. 414). Now the middlemost estimate is 1207 lb., and the weight of the dressed ox proved to be 1198 lb.; so the *vox populi* was in this case 9 lb., or 0.8 per cent., of the whole weight too high. The distribution of the estimates about their middlemost value was of the usual type, so far that they clustered closely in its neighborhood and because rapidly more sparse as the distance from it increased [Diagram 1 found on p. 365]. But they were not scattered symmetrically. One quarter of them deviated more than 45 lb. above the middlemost (3.7 per cent.), and another quarter deviated more than 29 lb., below it (2.4 per cent.), therefore the range of the two middle quarters, that is, of the middlemost half, lay within those limits. It would be an equal chance that the estimate written

	s	Centile			
Excess of observed over normal	Normal p.e. = 37	Observed deviates from 1207 lbs.	Estimates in lbs.	Degree of the length of array 0°–100°	
+43	-90	-133	1074	°5	
+28	_70	98	1109	10	
+24	-57	81	1126	15	
+13	-46	-59	1148	20	
+8	_37	-45	1162	q1 25	
+4	-29	-33	1174	30	
_					

Table 1. Distribution of the estimates of the dressed weight of a particular living ox, made by 787 different persons.

35	1181	-26	-21	+5
40	1188	-19	-14	+5
45	1197	-10	_7	+3
m 50	1207	0	0	0
55	1214	+7	+7	0
60	1219	+12	+14	_2
65	1225	+18	+21	_3
70	1230	+23	+29	6
q <sub>3</sub> 75	1236	+29	+37	8
80	1243	+36	+46	-10
85	1254	+47	+57	-10
90	1267	+52	+70	-18
95	1293	+86	+90	_4

q1, q3, the first and third quartiles, stand at 25° and 75° respectively.

m, the median or middlemost value stands at 50°.

The dressed weight proved to be 1198 lbs.

on any card picked at random out of the collection lay within or without those limits. In other words, the "probable error" of a single observation may be reckoned as  $\frac{1}{2}$  (45+29), or 37 lb. (3.1 per cent.). Taking this for the p.e. of the normal curve that is best adapted for comparison with the observed values, the results are obtained which appear in above table, and graphically in the diagram [see Diagram 1].

The abnormality of the distribution of the estimates now becomes manifest, and is of this kind. The competitors may be imagined to have erred *normally* in the first instance, and then to have magnified all errors that were negative and to have minified all those that were positive. The lower half of the "observed" curve agrees for a large part of its range with a normal



Diagram 1. From the tabular values. The continuous line is the normal curve with p.e. = 37. The broken line is drawn from the observations

The broken line is drawn from the observations. The lines connecting them show the differences between the observed and the normal.

curve having the p.e. = 45, and the upper half with one having its p.e. = 29. I have not sufficient knowledge of the mental methods followed by those who judge weights to offer a useful opinion as to the cause of this curious anomaly. It is partly a psychological question, in answering which the various psychophysical investigations of Fechner and others would have to be taken into account. Also the anomaly may be partly due to the use of a *small* variety of different methods, or formulae, so that the estimates are not homogeneous in that respect.

It appears then, in this particular instance, that the vox populi is correct to within 1 per cent. of the real value, and that the individual estimates are abnormally distributed in such a way that it is an equal chance whether one of them, selected at random, falls within or without the limits of -3.7 per cent. and +2.4 per cent. of their middlemost value.

This result is, I think, more creditable to the trustworthiness of a democratic judgment than might have been expected.

The authorities of the more important cattle shows might do service to statistics if they made a practice of preserving the sets of cards of this description, that they may obtain on future occasions, and loaned them under proper restrictions, as these have been, for statistical discussion. The fact of the cards being numbered makes it possible to ascertain whether any given set is complete.

Francis Galton

In his first paper we read:

How can the right conclusion be reached, considering that there may be as many different estimates as there are members? That conclusion is clearly not the average of all the estimates, which would give a voting power to "cranks" in proportion to their crankiness. One absurdly large or small estimate would leave a greater impress on the result than one of reasonable amount, and the more an estimate diverges from the bulk of the rest, the more influence would it exert. I wish to point out that the estimate to which least objection can be raised is the middlemost estimate, the number of votes that it is too high being exactly balanced by the number of votes that it is too low.

However, in discussing Galton's ox example, Surowiecki says that Galton calculated the mean not the median to get an estimate of 1,197 pounds for the true value of 1,198 pounds. In a letter to the editor, 1,197 is an approximation to the mean obtained by averaging the entries in the second column of Galton's Table 1. Even though this gives a better estimate, Galton defends his argument that, in this kind of problem, the median should be used. On the other hand Surowiecki seems to use the average throughout.

The concern of the effect of the "cranks" also occurred to us when we looked at the Jelly Bean Challenge on the book's <u>website</u>. The challenge offers an American Express gift certificate in the amount of one-hundred dollars to the person who best estimates the number of beans in a jar shown from two angles on the website.



Front View Approximate dimensions of jar: 10" high x 7" at the widest part x 4 3/4" deep



Side View Approximate dimensions of jar: 10" high x 7" at the widest part x 4 3/4" deep

The contest ended August 16 but the winner has not been announced. This kind of contest would make an interesting activity for a statistics class and could lead to a discussion of whether the mean or the median of the estimates gives a better estimate for the true number of Jelly Beans.

#### **DISCUSSION QUESTIONS:**

(1) What are the arguments for and against using the median of the predictions as the predictor? What are they for using the mean? Which would you use?

(2) Suppose that people are answering a common question with two possible answers, one false and one true, and that the average probability that each voter will answer correctly exceeds 50 percent. The Condorcet Jury Theorem holds that if each member of the group is answering independently, the probability of a correct answer, by a majority of the group, increases toward certainty as the size of the group increases.

If each person is more likely than not to err, then the theorem's prediction is reversed: the probability of a correct answer, by a majority of the group, decreases toward zero as the size of the group increases.

What does this theorem say about majority opinion as compared to individual opinion? See if you can prove the Condorcet Jury Theorem.

#### Answer to the "lost boarding pass" puzzle.

First we consider a smaller example:

passenger	1	2	3	4	5	6	7	8	9	10
Assigned seat	6	3	8	7	10	4	9	2	5	1
Final seat	7	3	8	9	10	4	1	2	5	6

Passenger 1 has lost his boarding pass and so randomly chooses a seat. He chooses seat 7 which was assigned to passenger 4. Then passengers 2 and 3 sit in their assigned seats (3,8) and passenger 4 finds his seat taken so randomly chooses a seat from the seats that are free which are the seat of passenger 1 (6) and the assigned seats for passengers behind him in the line (10, 4, 9, 2, 5 1). He chose seat 9 which was assigned to passenger 7. Thus passengers 5 and 6 get their assigned seats (10,4) and 7 must choose a seat randomly from passenger 1's seat (6) and seats assigned to those after him (2,5,1). Passenger 7 chooses seat 1 which was assigned to passenger 10. Now passengers 8 and 9 will get thier assigned seats (9,2) and passenger 10 will have to take passenger 1 seat (6) and everyone has a seat. Had 7 chosen passenger 1's seat then passenger 10 would have his assigned seat. Since passenger 7's choice was a random choice, given that he chose either the seat assigned to the first or last passenger the probability that he chose the seat assigned to passenger 1 is 1/2, so this is the probability that the last passenger gets his assigned seat.

As the above example shows, when the first passenger chooses a random seat, either he chooses the seat assigned to

him or the last passenger or he sets in motion a sequence of passengers who find their seats occupied and have to make random choices among the seats available. This sequence continues until a passenger's random choice is either the seat assigned to the first or the last passenger. This must happen before the next-to -last passenger boards since if it does not happen until then, then he would have three seats to choose from: his seat, that of the first passenger, and the last passenger's seat. But that is impossible since he and the last passanger are the only passengers without seats.

Thus one and only one random choice will result in choosing either the first or last passangers seat. Given that this happens there is an equal chance that it is the first or the last person's seat. Thus the probability that the last person gets the seat assigned to him/her is 1/2.

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